

Lecture 1:  
Introduction to Decision Making Theory

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BIS4435

Choice Problem and Preference Relations

Utility Function

Multicriteria Decision Making

Complexity and Uncertainty

The Structure of Decisions

The Three Phases of Decision Making

Supporting Decisions in Business

# THE CHOICE PROBLEM and PREFERENCE RELATION

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- ① *Total*: defined for all elements of the set
- ② *Transitive*: If  $a \succsim b$  and  $b \succsim c$ , then  $a \succsim c$

**Indifference**  $a \sim b$ , when  $a \succsim b$  and  $b \succsim a$

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The preference relation can help us to order the set

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## Example

You have two job offers: **Job1** with a salary \$18K and **Job2** with \$30K. Most of us would choose **Job2** because:

$$u(\text{Job2}) = \$30,000 > u(\text{Job1}) = \$18,000$$

# MULTICRITERIA DECISION MAKING

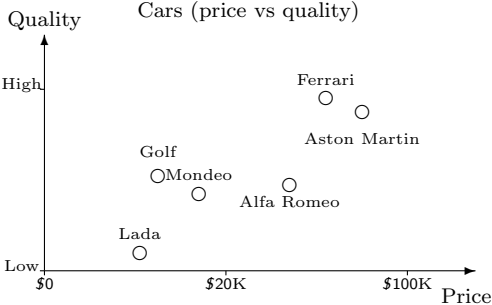
Let **Job1** be in **City1** and **Job2** be in **City2**. Suppose now that **City1** is located near the sea, has a good climate, nice restaurants, cheap food and your girl/boy–friend lives there. And let **City2** has none of these.

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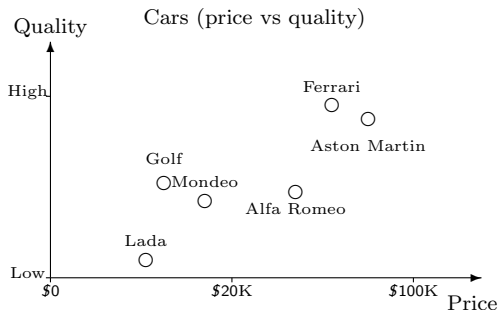
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- What will be your decision?
- How many objectives you considered?
- Has learning new information changed your decision?

# MULTICRITERIA UTILITY



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We could use the following utility:

$$U = \frac{\text{Quality}}{\text{Price}}$$

How to choose between  
Mondeo and Aston  
Martin?

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- Multiplicative utility

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# PROBLEMS WITH RATIONAL APPROACH

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Which one would you choose?

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- Psychologists showed that people match the probability of a reward in their choice behaviour.
- Nevertheless, people do not always choose what seems rational

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Consider a chess game.

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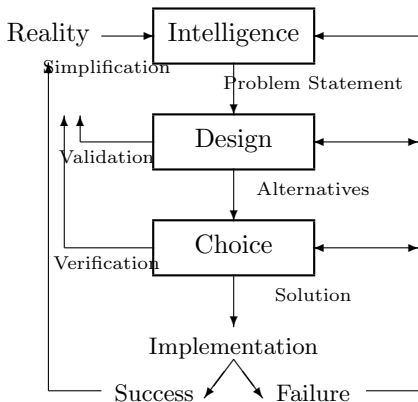
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# THE STRUCTURE OF DECISIONS

Herbert Simon introduced the idea of **structured** (programmable) and **unstructured** (nonprogrammable) decisions.

Structured	Semi-structured	Unstructured
goals defined	...	the outcomes are uncertain
procedures are known	...	appear in unique context
information is obtainable and manageable	...	the resources are hard to assess

# THE THREE PHASES OF DECISION MAKING



Simon (1977)



# DECISIONS IN BUSINESS

Economy is hard to predict, but there are some trends and cycles. If we can detect them, then we shall be able to make better decisions (better than our competitors). Thus, DSS should provide us with:

- More information (knowledge) of the domain (market, resources)
- Better definition of the utility (objectives of the decision)
- A set of alternative actions (solutions)
- Prediction of the possible outcomes of the solutions (expected utilities)

# SUPPORTING THE INTELLIGENCE PHASE

According to three main sources of information:

**Internal** using DBMS, MIS and custom built data retrieval

**External** using external DBs (online, from gov-nt, etc)

**Personal** more specific (relevant) set of parameters

The tools for analysis and visualisation of data are very important (statistical analysis, pattern recognition, self-organising maps, etc).

# SUPPORTING THE DESIGN PHASE

The solution to a problem (or a set of alternative solutions) can be proposed using various techniques:

- Analytical solutions (maths)
- Decision trees
- Expert systems (rule or case-based, fuzzy, etc)
- Optimisation (e.g. genetic algorithms)
- Models and simulations

# SUPPORTING THE CHOICE PHASE

The proposed solutions may have problems:

- Not palatable
- None of the solutions seem to have clear advantage
- The world (situation) has already changed

Final decision must be made and documented.