

Common Lisp Implementation of FastICA

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BLIND SOURCE SEPARATION (or ICA)

$$\mathbf{X} = (x_1, \dots, x_m)^T, \mathbf{Y} = (y_1, \dots, y_n)^T$$

$$\mathbf{Y} = \mathbf{W}\mathbf{X}$$

Assuming:

1. $P(x_1, \dots, x_m) = P(x_1) \cdots P(x_m)$
2. $\forall i$ but one $P(x_i)$ are non-Gaussian

Find $\mathbf{A} \approx \mathbf{W}^{-1}$ such that

$$\mathbf{A}\mathbf{Y} \approx \mathbf{X}$$

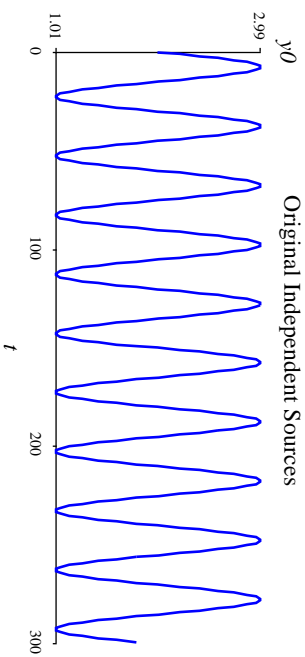
Common Lisp Implementation

ICA.lisp (5K) + PCA.lisp (8K) + Matrices.lisp (10K) = 23K of code:

```
(defun one-unit-fica (X &key .....)  
  (do* ((m (num-rows X))  
        (w (find-one-weight X nil)  
            (find-one-weight X ws)))  
        (ws (list w) (push w ws)))  
    ((= (length ws) m)  
     (let ((W (make-array (list m m))))  
       (dotimes (i m W)  
         (dotimes (j m)  
           (setf (aref W i j)  
                 (aref (nth j ws) i 0)))))))
```

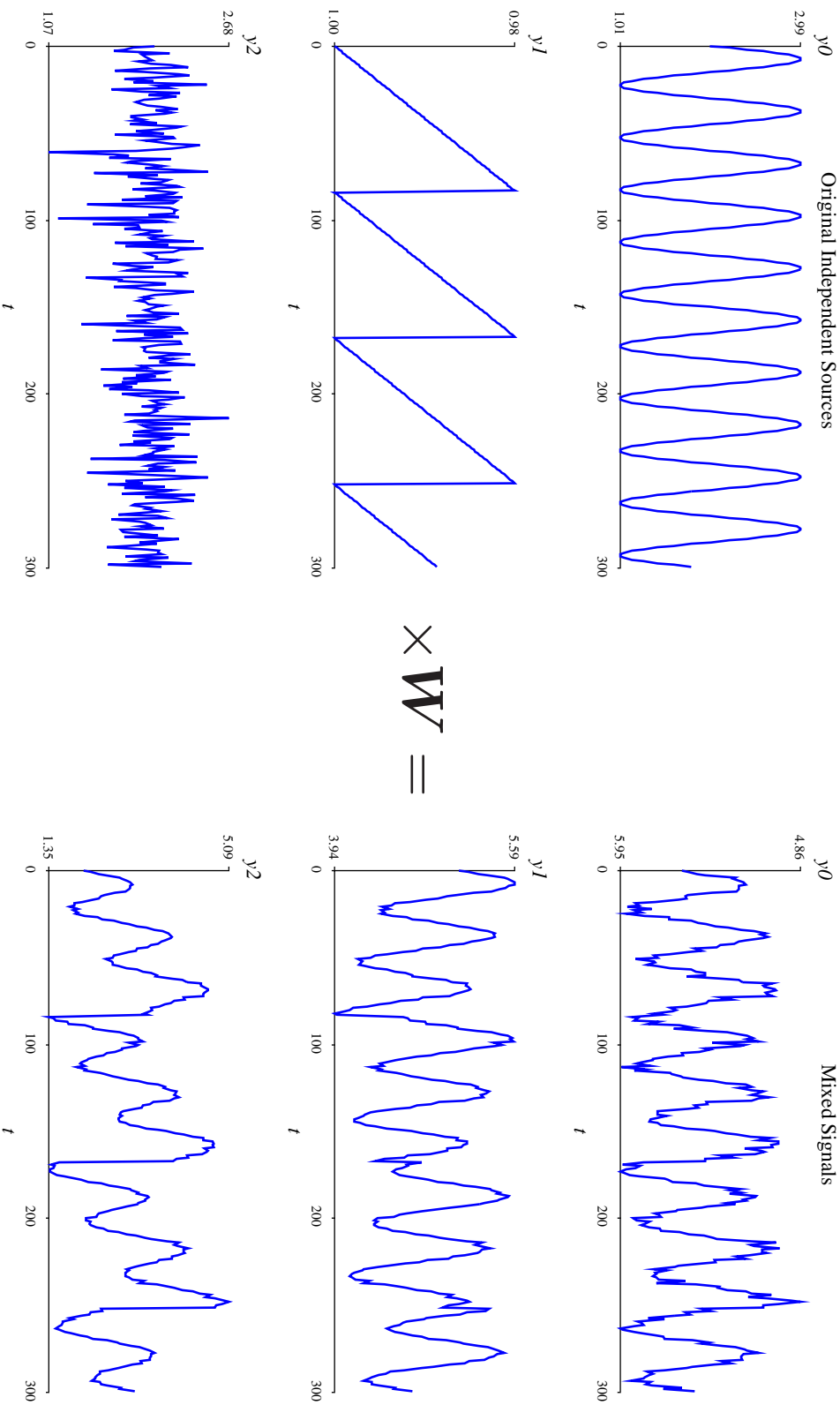
MIXING SOURCES

Original Independent Sources



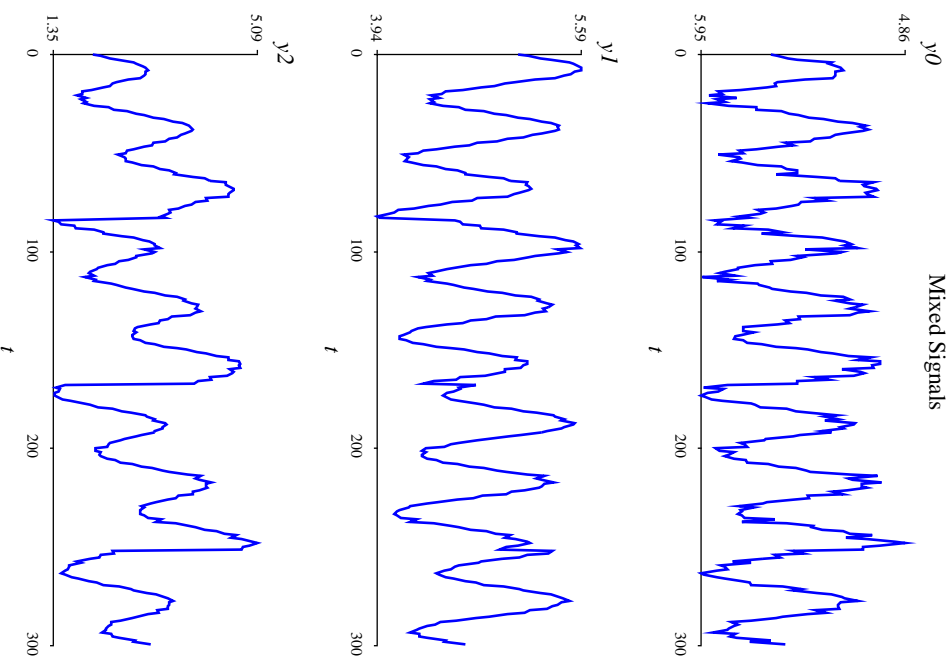
$$\times W =$$

Mixed Signals



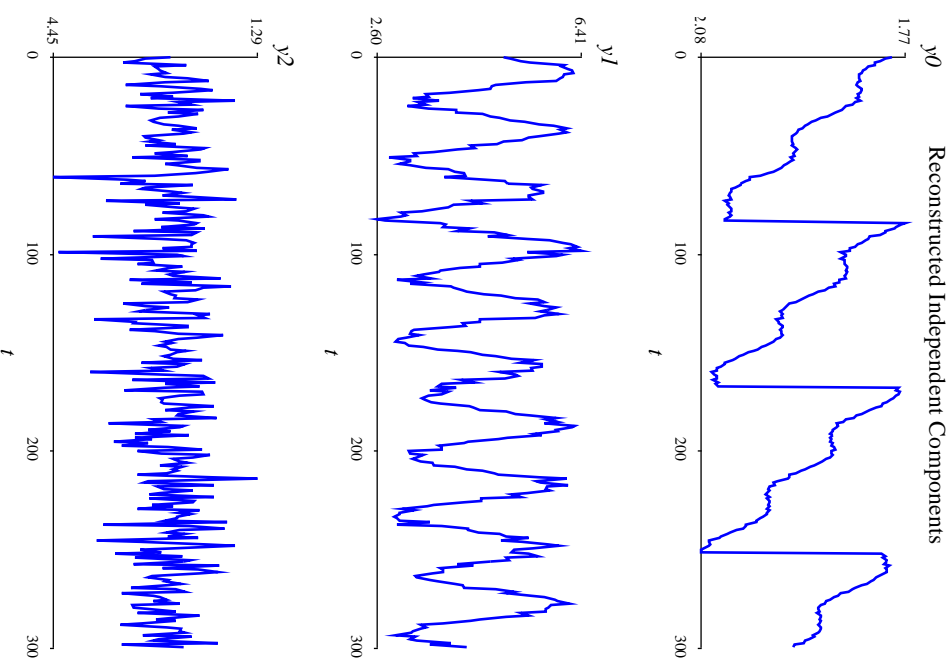
DEMIXING SIGNALS

Mixed Signals



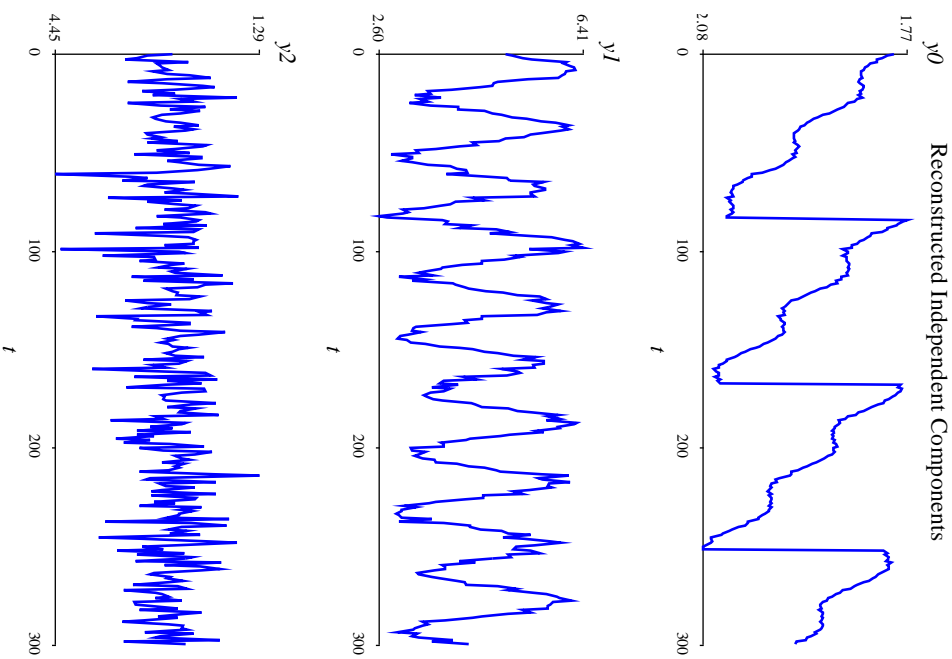
$$\times \mathbf{A} =$$

Reconstructed Independent Components



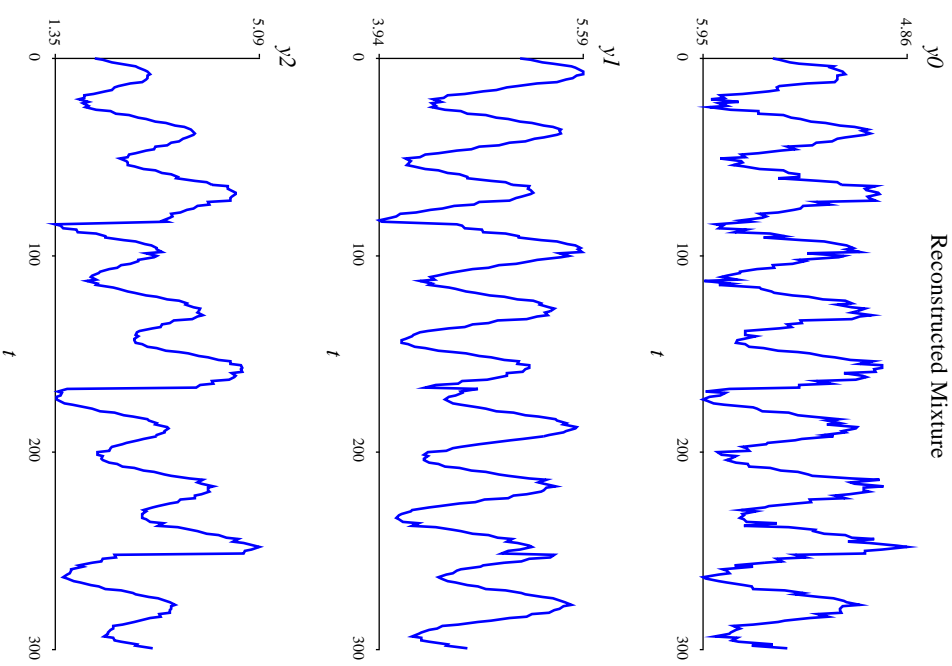
RECONSTRUCTING MIXTURE

Reconstructed Independent Components



$$\times \mathbf{A}^{-1} =$$

Reconstructed Mixture



FUTURE WORK

- Use ICA output as an input to Bayesian learning agents (perception with reduction of dimensions and minimal loss of information):

$X \in \mathbf{R}^n$ perception inputs

$Y \in \mathbf{Z}$ set of actions

$X \rightarrow S \in \mathbf{R}^m$ reduce dimensions (ICA)

$$P(Y | S, U) = \alpha P(Y, S, U)$$

- Encourage MSc students to use ICA in their projects in Business Information Systems programme.